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Distributed probabilistic data association detector with turbo base-station cooperations in multi-user multi-cell MIMO systems

Yufang Yin¹, Gangjun Li¹ and Hua Wei^{2*}

Abstract

We address the severe interference condition with unity frequency re-use factor in each cell and propose a novel distributed receiver for reliable detection of the uncoded data transmitted in multi-user multi-cell multiple input, multiple output (MIMO) systems. The new algorithm employs distributed probabilistic data association (PDA) with turbo base-station (BS) cooperations (PDA-TB). From a Bayesian point of view, we modify the original complex PDA detector to incorporate the a priori probability, which makes the complex PDA detector applicable to turbo processing: the soft information is extracted using PDA algorithm at local BS and then used as the a priori probability for further detection at neighboring BSs. Final soft decision is made after the algorithm converges. In this way, the benefit of macro-diversity is achieved and the inter-cell interferences are mitigated. In heavy interference condition, the proposed algorithm outperforms the distributed PDA aided soft combining (PDA-SC) and achieves the near optimal performance. Meanwhile, low complexity is maintained due to the rapid convergence.

Keywords: PDA, MIMO, Turbo detector, BS cooperations

1 Introduction

To design the mobile communication systems, one has to face two key challenges: fading and interference. Both of them restrict the system coverage and capacity. Especially in a multi-user multi-cell multiple input, multiple output (MIMO) system, the gain of MIMO technique is determined by the inter-cell co-channel interference (CCI). Consider a severe interference condition with unit frequency re-use factor where, at the cell boundary areas, mobile stations (MSs) transmit the signals which can be detected by the surrounding base stations (BSs). The conventional non-cooperative BS detects the desired MS signals independently using local received data. Moreover, the co-channel users' signals are considered as interference and then degrade the system throughput. However, in the cooperative system, those interference signals are dealt with specific tools such as virtual MIMO and then are treated more like the useful information to jointly

detect the MS signals. In this way, the number of co-channel links can be maximized so as to optimize the system capacity.

In the centralized BS cooperations, the complexity of the general multi-user multi-cell MIMO detection grows exponentially with the number of antennas. It raises a question of scalability and motivates the search for simplified suboptimal algorithms. To solve this problem, it is straightforward to distribute, across a network of interacting BSs, the global uplink task of demodulating all users' data symbols [1]. Each BS individually performs local computations and then passes the processed soft information to immediate neighbors for further processing. Distributed BS cooperations were discussed in recent literatures [2, 5–7]. Among them, Yang [2] proposed a simple soft combining method through which the soft information, calculated in parallel at different BSs, is statistically aggregated to make the final decision.

Besides the conventional distributed schemes, it is very natural to try and apply well-known turbo principle [1], which has been employed in turbo equalization [3, 4], Bayesian data integration [7, 8], and turbo BS cooperations [5–7, 9]. Turbo principle was originated from turbo

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decoding, and in the context of cooperative communication systems, it explores the synergy from distributed detections on symbols and combines the soft (probabilistic) detection in a turbo fashion to achieve greater performance improvement. The implementation of turbo cooperations separates the joint detections into commonly two or possibly more connected units (BSs), and the a posteriori probability (APP) of symbols are calculated at each unit with the extrinsic information obtained at other units as the a priori probability. The processes then iterate among the units until the convergence of the APPs. The output of the turbo BS cooperation is a near optimal approximation of true APPs, and Mayer [10] illustrated the explicit connection to Turbo-decoding and message-passing algorithm.

To obtain the soft information through local detection, many low-complexity algorithms have been investigated as alternative designs for optimal maximum a posteriori probability (MAP) solution. Among them, probabilistic data association (PDA) has attracted many attentions and shown to provide a near-optimal multi-user detection (MUD) [11, 12] performance in the context of Code Division Multiple Access (CDMA) [16]. The basic idea of the PDA is to approximate the Gaussian mixture with a single Gaussian distribution, a concept seemingly simple yet very effective in practice. Another appealing advantage of the PDA is that it is soft in nature and thus applicable to turbo BS cooperations. Moreover, [17] indicated that the larger the number of users, the better performance achievable due to the Gaussian approximation. This makes PDA attractive for a MUD scenario with large number of interferers.

The soft combining in [2] is based on complex PDA (CPDA) algorithm [13–15], which matches the full parameters of the complex Gaussian distribution and outperforms the approximated CPDA used in our previous work [4]. However, the original form of CPDA assumes uniform (or non-informative) prior and then does not incorporate practical prior knowledge. As a result, empirical information obtained in other BSs is lost and then the overall performance is somehow degraded. It implies that further performance improvement over the PDA-SC algorithm is possible if the prior information can be carefully manipulated.

In this paper, we investigate the distributed PDA detector with turbo BS cooperations. We modify the structure for original CPDA, where the a priori probability is appropriately incorporated. This modification considers the soft information obtained from neighboring BSs and then makes PDA readily applicable to turbo BS cooperations. We also provide the performance of the proposed algorithm by simulations.

The remaining of the paper is organized as follows. The problem is formulated in Section 2. The distributed PDA

with turbo BS cooperations is described in Section 3. Simulation results are presented in Section 4, and finally, the conclusions are drawn in Section 5.

2 Problem formulation

Consider the uplink in a multi-user multi-cell system, where the uncoded data is transmitted from N_m mobile stations (MS) to N_b BSs. Each MS has N_t transmit antennas, and each BS is equipped with N_r receive antennas. In the cell edges, assume the signals transmitted by MSs are in the detectable range (DR) of N_b BSs and then can be detected by all the BSs. We are interested in this extremely challenging scenario and discuss the signal model as follows.

The signal received at BS_{*i*} is

$$\mathbf{y}^i = \sum_{l=1}^{N_m} \mathbf{H}_l^i \mathbf{x}_l + \mathbf{n}^i, \quad (1)$$

where \mathbf{y}^i is the $N_r \times 1$ vector of symbols received at BS_{*i*}, \mathbf{H}_l^i is the $N_r \times N_t$ complex channel matrix between MS_{*l*} and BS_{*i*}, \mathbf{x}_l is the $N_t \times 1$ vector of symbols transmitted from MS_{*l*}, and \mathbf{n}^i is the complex Gaussian noise with zero mean and covariance matrix $\sigma_n^2 \mathbf{I}_{N_r}$. This signal model can be further formulated as a virtual MIMO system as the following

$$\mathbf{y}^i = \mathbf{H}^i \mathbf{x} + \mathbf{n}^i, \quad (2)$$

where $\mathbf{H}^i = [\mathbf{H}_1^i, \dots, \mathbf{H}_{N_m}^i]$, $\mathbf{x} = [(\mathbf{x}_1)^\top, \dots, (\mathbf{x}_{N_m})^\top]^\top$. Assume \mathbf{H}^i and σ_n^2 are known.

To mitigate the inter-cell interferences, a natural way is to perform the joint detection with BS cooperations. Our objective is to determine x_k , $k = 1, \dots, N_m \times N_t$ given received signals \mathbf{y}^i , $i = 1, \dots, N_b$. From a Bayesian point of view, the marginal APP is calculated to make the decision,

$$\hat{x}_k = \arg \max_{\alpha_m} p(x_k = \alpha_m | \mathbf{y}^{1:N_b}) \quad (3)$$

where $\mathbf{y}^{1:N_b} = \mathbf{y}^1, \dots, \mathbf{y}^{N_b}$ and α_m is the m -th element of the M -ary constellation A .

3 PDA-based turbo BS cooperations

The goal of our soft detector is to obtain $p(x_k | \mathbf{y}^{1:N_b})$ and then detect the transmitted symbol x_k . One way to reduce the complexity is to perform distributed detection, using local \mathbf{y}^i to calculate $p(x_k | \mathbf{y}^i)$ and approximating $p(x_k | \mathbf{y}^{1:N_b})$ through BS cooperations. This motivates us to exploit distributed detector with BS cooperations, and it is very natural to apply well-known turbo principle to achieve near optimal performance.

$p(x_k | \mathbf{y}^i)$ can be obtained easily if $p(\mathbf{y}^i | x_k)$ is known since

$$p(x_k | \mathbf{y}^i) = \frac{p(\mathbf{y}^i | x_k) p(x_k)}{\sum_{x_k} p(\mathbf{y}^i | x_k) p(x_k)}. \quad (4)$$

However, to obtain $p(\mathbf{y}^i|x_k)$, marginalization must be performed as

$$p(\mathbf{y}^i|x_k) = \sum_{\mathbf{x}_{-k}} p(\mathbf{y}^i|\mathbf{x})p(\mathbf{x}_{-k}), \quad (5)$$

where \mathbf{x}_{-k} represents a $(N_t N_m - 1) \times 1$ vector that contains all data symbols except x_k . Apparently, the optimal MAP solution of (3) is of complexity exponential increasing of $N_t N_m$ and thus computationally infeasible for large systems. Notice that $\sum_{\mathbf{x}_{-k}} p(\mathbf{y}^i|\mathbf{x})p(\mathbf{x}_{-k})$ is the mixture of Gaussian distribution; we can further simplify the receiver by approximating the mixture Gaussian by a single Gaussian. This motivates us to employ PDA detector at every BS. In addition, modification is made to allow PDA detector to accept prior information and then workable in turbo BS cooperations.

The proposed algorithm is then named by PDA-TB. It follows the Bayesian rule and turbo principle that BS*i* individually perform local PDA computation with \mathbf{y}^i , and then outputs the soft information as the a priori probability for neighboring BSs to continue their PDA detections until the APPs calculated at different BSs get convergence.

3.1 The complex PDA detector

3.1.1 $N_m N_t \leq N_r$

Given that $(\mathbf{H}^i)^H \mathbf{H}^i$ is invertible, (2) can be rewritten as the decorrelated signal model:

$$\tilde{\mathbf{y}}^i = [(\mathbf{H}^i)^H \mathbf{H}^i]^{-1} (\mathbf{H}^i)^H \mathbf{y}, \quad (6)$$

and it is equivalent to have

$$\tilde{\mathbf{y}}^i = \mathbf{x} + \tilde{\mathbf{n}}^i \quad (7)$$

$$= x_k \mathbf{e}_k + \sum_{j \neq k} x_j \mathbf{e}_j + \tilde{\mathbf{n}}^i \quad (8)$$

$$\triangleq x_k \mathbf{e}_k + \mathbf{v}_k^i, \quad (9)$$

where $\tilde{\mathbf{n}}^i$ is a Gaussian noise with zero mean and covariance $\Lambda = \sigma_n^2 [(\mathbf{H}^i)^H \mathbf{H}^i]^{-1}$, \mathbf{e}_k is a column vector with a 1 in the k th element and zeros elsewhere, and vector $\mathbf{v}_k^i = \sum_{j \neq k} x_j \mathbf{e}_j + \tilde{\mathbf{n}}^i$ has a multimodal Gaussian mixture distribution.

Since the signal model is complex-valued, the complex formulation of PDA is preferred. The basic idea behind complex PDA is to approximate \mathbf{v}_k^i as a single Gaussian distribution with the matched mean $E(\mathbf{v}_k^i)$, covariance $V(\mathbf{v}_k^i)$, and pseudo-covariance $U(\mathbf{v}_k^i)$ [15],

$$E(\mathbf{v}_k^i) = \sum_{j \neq k} \tilde{x}_j \mathbf{e}_j, \quad (10)$$

$$V(\mathbf{v}_k^i) = \sum_{j \neq k} V(x_j) \mathbf{e}_j \mathbf{e}_j^T + \sigma^2 [(\mathbf{H}^i)^H \mathbf{H}^i]^{-1}, \quad (11)$$

$$U(\mathbf{v}_k^i) = \sum_{j \neq k} U(x_j) \mathbf{e}_j \mathbf{e}_j^T, \quad (12)$$

where

$$\tilde{x}_j = \sum_{x_j \in A} x_j p(x_j | \mathbf{y}^i), \quad (13)$$

$$V(x_j) = \sum_{x_j \in A} (x_j - \tilde{x}_j)(x_j - \tilde{x}_j)^* p(x_j | \mathbf{y}^i), \quad (14)$$

$$U(x_j) = \sum_{x_j \in A} (x_j - \tilde{x}_j)(x_j - \tilde{x}_j)^T p(x_j | \mathbf{y}^i). \quad (15)$$

This approximation is called data association.

Let

$$\mathbf{w} = \tilde{\mathbf{y}}^i - x_k \mathbf{e}_k - \sum_{j \neq k} \tilde{x}_j \mathbf{e}_j \quad (16)$$

and

$$\phi(x_k^i) \triangleq \exp \left(- \left(\begin{matrix} R(\mathbf{w}) \\ I(\mathbf{w}) \end{matrix} \right)^T \Sigma_k^{-1} \left(\begin{matrix} R(\mathbf{w}) \\ I(\mathbf{w}) \end{matrix} \right) \right) \quad (17)$$

$$\Sigma_k \triangleq \begin{pmatrix} R(V(\mathbf{v}_k^i) + U(\mathbf{v}_k^i)) & I(-V(\mathbf{v}_k^i) + U(\mathbf{v}_k^i)) \\ I(V(\mathbf{v}_k^i) + U(\mathbf{v}_k^i)) & R(V(\mathbf{v}_k^i) - U(\mathbf{v}_k^i)) \end{pmatrix} \quad (18)$$

where $R(*)$ and $I(*)$ represent the real and imaginary part of a complex variable. The original complex PDA assumes the uniform or non-informative prior [15], and then, the APP of x_k is approximated by the likelihood function. To develop a general complex PDA detector, we incorporate the prior information $p(x_k^i)$ and calculate the APP of x_k by

$$p(x_k | \mathbf{y}^i) \approx \frac{\phi(x_k^i) p(x_k^i)}{\sum_{x_j \in A} \phi(x_j^i) p(x_j^i)}, \quad (19)$$

and the symbol log-likelihood ratio (LLR) Λ_k^i by

$$\Lambda_k^i \triangleq (\lambda_0^i, \lambda_1^i, \dots, \lambda_{M-1}^i) \quad (20)$$

with

$$\lambda_m^i = \log \frac{p(\mathbf{y}^i | x_k = \alpha_m)}{p(\mathbf{y}^i | x_k = \bar{\alpha}_m)} \quad (21)$$

$$= \log \frac{p(x_k = \alpha_m | \mathbf{y}^i) / p(x_k^i = \alpha_m)}{p(x_k = \bar{\alpha}_m | \mathbf{y}^i) / p(x_k^i = \bar{\alpha}_m)} \quad (22)$$

where $m = 0, \dots, M - 1$ is the index of the elements in symbol constellation A .

Since (19) is only an approximation to the true APP, the PDA detector will, after one sweep of update from $k = 1 : N_t N_m$, start another sweep until the APPs converge. In the end, the detection is performed as

$$\hat{x}_k = \arg \max_{x_k \in A} p(x_k | \mathbf{y}^i) \quad (23)$$

The complexity of PDA at each BS per iteration is on the order of $O[(N_m N_t)^3]$. The above procedure is summarized in Table 1.

Table 1 The summary of PDA detector

-
- 1) Initialization: $p(x_k|\mathbf{y}^1) = 1/M, k = 1, \dots, N_t N_m$.
 - 2) Decorrelated model: Calculate $\tilde{\mathbf{y}}^j$ according to (6)
 - 3) For $k = 1 : N_t N_m$
 - Data association: Compute $E(\mathbf{v}_k^j), V(\mathbf{v}_k^j)$ and $U(\mathbf{v}_k^j)$ from (10), (11) and (12).
 - Probability update: Calculate APPs $p(x_k|\mathbf{y}^j)$ according to (20).
 - 4) Convergence testing: If the APPs converge, go to 5). Otherwise, go back to 3).
 - 5) LLR updating: Update LLR Λ_k^j according to (21).
 - 6) Detection: Detect x_k according to (23).
-

3.1.2 $N_m N_t > N_r$

Given that the total number of transmit antennas is smaller than the number of receive antennas, $(\mathbf{H}^i)^H \mathbf{H}^i$ is not invertible any more. In the case of non-decorrelated model, (2) is rewritten as

$$\mathbf{y}^i = \mathbf{h}_k^i x_k + \sum_{j \neq k} \mathbf{h}_j^i x_j + \mathbf{n} \quad (24)$$

$$\triangleq \mathbf{h}_k^i x_k + \mathbf{u}_k^i, \quad (25)$$

where \mathbf{h}_k^i is the k -th column of \mathbf{H}^i and \mathbf{u}_k^i is the equivalent interference plus noise. Then, PDA algorithm can be obtained using a similar derivation as in decorrelated model discussed in Section 3.1.1.

3.2 Turbo BS cooperations

For simple illustration, assume that there are two BSs in the system: BS₁ and BS₂. The following method can be easily extended to the case with $N_m \geq 3$. In turbo BS cooperations, LLR Λ_k^i is the soft information and exchanged among BSs iteratively until the APPs $p(x_k|\mathbf{y}^{1:2})$ converge. The detailed procedure is demonstrated in the following.

APP $p(x_k|\mathbf{y}^{1:2})$ can be further factorized as

$$p(x_k|\mathbf{y}^{1:2}) \propto p(x_k)p(\mathbf{y}^{1:2}|x_k) \quad (26)$$

$$\propto p(x_k)p(\mathbf{y}^1|x_k)p(\mathbf{y}^2|x_k) \quad (27)$$

assuming \mathbf{y}^1 and \mathbf{y}^2 are independent given x_k . Initially, assume $p(x_k) = 1/M$. At BS₁, use $p(x_k^1) = p(x_k)$ with data \mathbf{y}^1 to approximate APP $p(x_k|\mathbf{y}^1)$ and LLR Λ_k^1 . Then at BS₂, $p(x_k)p(\mathbf{y}^1|x_k)$ is equivalent to the a priori probability $p(x_k^2)$. Given $p(x_k) = 1/M$ is a non-informative prior, we set $p(x_k^2) \propto p(\mathbf{y}^1|x_k)$. Specifically, $p(x_k^2 = \alpha_m) = \frac{\exp(\lambda_m^1)}{1 + \sum_{p=1}^{M-1} \exp(\lambda_p^1)}$. In another word, the LLR Λ_k^1 computed at BS₁ is treated as soft information and set as the a priori probability $p(x_k^2)$ at BS₂. With the local received data \mathbf{y}^2 and the prior information $p(x_k^2)$, BS₂ performs the PDA detection and produces the approximated APP $p(x_k|\mathbf{y}^{1:2})$.

Again, the LLR Λ_k^2 needs to be updated according to

$$\lambda_m^2 \triangleq \log \frac{p(\mathbf{y}^2|x_k = \alpha_m)}{p(\mathbf{y}^2|x_k = \alpha_0)} \quad (28)$$

where

$$p(\mathbf{y}^2|x_k) \propto \frac{p(\mathbf{y}^{1:2}|x_k)}{p(\mathbf{y}^1|x_k)} \propto \frac{p(x_k|\mathbf{y}^{1:2})}{p(x_k^2)}. \quad (29)$$

Before moving to the next step, check first the gap between $p(x_k|\mathbf{y}^{1:2})$ and $p(x_k|\mathbf{y}^1)$. If the difference is small enough, the algorithm can be stopped and $p(x_k|\mathbf{y}^{1:2})$ is used to make the final decision on x_k . Otherwise, this LLR Λ_k^2 is passed to BS₁ as $p(x_k^1)$, and then, turbo processing is continued until the APPs converge. LLR is updated at each BS by

$$p(\mathbf{y}^i|x_k) \propto \frac{p(x_k|\mathbf{y}^{1:2})}{p(x_k^i)}. \quad (30)$$

The summary of proposed turbo BS cooperations using distributed PDA is in Table 2.

3.3 Soft information exchange

Assume there is an idealized backbone connecting all the BSs and the soft information Λ_k^i s are exchanged among BSs in a turbo fashion. After the APP converges, the soft decision is sent to each user's home BS.

4 Simulation results

For ease of illustration, we assume first $N_b = 2, N_t = 1$ in the system and a BPSK modulation for the transmitted data. And it is straightforward to extend those assumptions to the case with $N_b > 2, N_t > 1$ and high-order modulations. Moreover, we also offer the the results for those general cases with $N_b > 2, N_t > 1$.

In the simulation, \mathbf{H}^i is flat rayleigh fading channels. The maximum iteration in PDA computation is 5 since PDA typically converges within 3~5 iterations [16]. However, the inner PDA iterations degrade the performance of

Table 2 Distributed PDA detector with turbo BS cooperations

-
- 1) Initialize at the 0th iteration
 - BS₁, set $p(x_k^1) = 1/M$ and calculate $p(x_k|\mathbf{y}^1)$ and Λ_k^1 according to Table 1 using local data \mathbf{y}^1 .
 - BS₂, set $p(x_k^2)$ based on Λ_k^1 , calculate $p(x_k|\mathbf{y}^{1:2})$ according to Table 1 using local data \mathbf{y}^2 , update Λ_k^2 by (28).
 - if $|p(x_k|\mathbf{y}^1) - p(x_k|\mathbf{y}^{1:2})| < \epsilon$, go to 3); otherwise go to 2).
 - 2) Iterate until APP $p(x_k|\mathbf{y}^{1:2})$ converges. And at the t -th iteration, perform for $i = 1 : 2$
 - according to Table 1, update $p(x_k|\mathbf{y}^{1:2})$ using data \mathbf{y}^i with prior $p(x_k^i)$ obtained from $\Lambda_k^s, s \neq i$.
 - update Λ_k^i according to (30).
 - 3) Detect x_k according to (3).
-

turbo processing [12] despite of the increasing complexity. Therefore, we investigate and conclude that in PDA-TB, the optimal number of inner PDA iteration is 0. In contrast, the inner PDA iterations are adaptive according to the convergence condition of CPDA, in both PDA-SC and PDA-JP. The maximum outer iteration in turbo processing is 3 based on the empirical data.

4.1 BER comparison

4.1.1 Illustration on the simple cases with $N_b = 2, N_t = 1$ and BPSK modulation

Figures 1 and 2 show the BER performance of the proposed PDA-TB algorithm and PDA aided soft combining (PDA-SC) [2]. ‘‘PDA-SC’’ is the distributed algorithm where the term ‘‘soft combining’’ means

$$p(x_k | \mathbf{y}^{1:N_b}) \approx \prod_{i=1}^{N_b} p(x_k | \mathbf{y}^i), \tag{31}$$

where the a priori probability $p(x_k^i)$ is non-informative. In those two figures, ‘‘PDA’’ denotes the PDA detection with local received data \mathbf{y}^1 ; ‘‘PDA-JP’’ indicates the joint processing in a centralized system by employing PDA algorithm directly on the received data $\mathbf{y}^{1:N_b}$; ‘‘SD-JP’’ indicates the sphere decoding with the joint processing. Among them, PDA-JP and SD-JP are centralized BS cooperations where a central processing unit collects the received data $\mathbf{y}^{1:N_b}$ and employs PDA or SD respectively to calculate directly the APP $p(x_k | \mathbf{y}^{1:2})$.

Without BS cooperations, ‘‘PDA’’ shows significant degradation compared with centralized or distributed BS

cooperations. PDA-JP obtains almost the same performance as SD-JP. ‘‘PDA-TB’’ achieves similar BER performance as PDA-SC if small number of users ($N_m = 4$) are in DR. However, if interference is severe and more users are in DR, say $N_b = 16$, PDA-TB is close to the optimal SD-JP and outperforms PDA-SC by 0.5dB at BER of 10^{-4} . Even in rand-deficient case showed in Figs. 3 and 4 where $N_m N_t = 2N_r$, PDA-TB outperforms PDA-SC by around 1dB at BER of 10^{-2} .

4.1.2 Illustration on general cases

The proposed algorithm can be extended to the scenarios with higher-order modulation schemes, arbitrary N_t or even $N_b > 2$.

Figure 5 shows the impact of modulation order when $N_m = 4, N_t = 1, N_b = 2$, and $N_r = 4$. As the modulation scheme changes from BPSK to 4QAM and 8QAM, the gain between PDA-TB and PDA-SC increases from almost 0, 0.3, and 1 dB at BER of 10^{-3} , respectively.

Figure 6 demonstrates the impact of the total number of streams which is equal to $N_m \times N_t$, when $N_b = 2$ and $N_r = N_m \times N_t$. As the total number of streams increases from 4 to 8 and 16, the gain of PDA-TB over PDA-SC is according to 0, 0.4, and 0.55 dB at BER of 10^{-4} . The simulation results demonstrate that the PDA-TB can achieve a slight gain over the PDA-SC when the system has a fixed stream number.

Figure 7 indicates that PDA-TB achieves about 2.2 dB gain while incorporating 3 base stations over 2. However, there is no obvious improvement if PDA-SC is used to involve 3 base stations rather than 2. Hence, we can

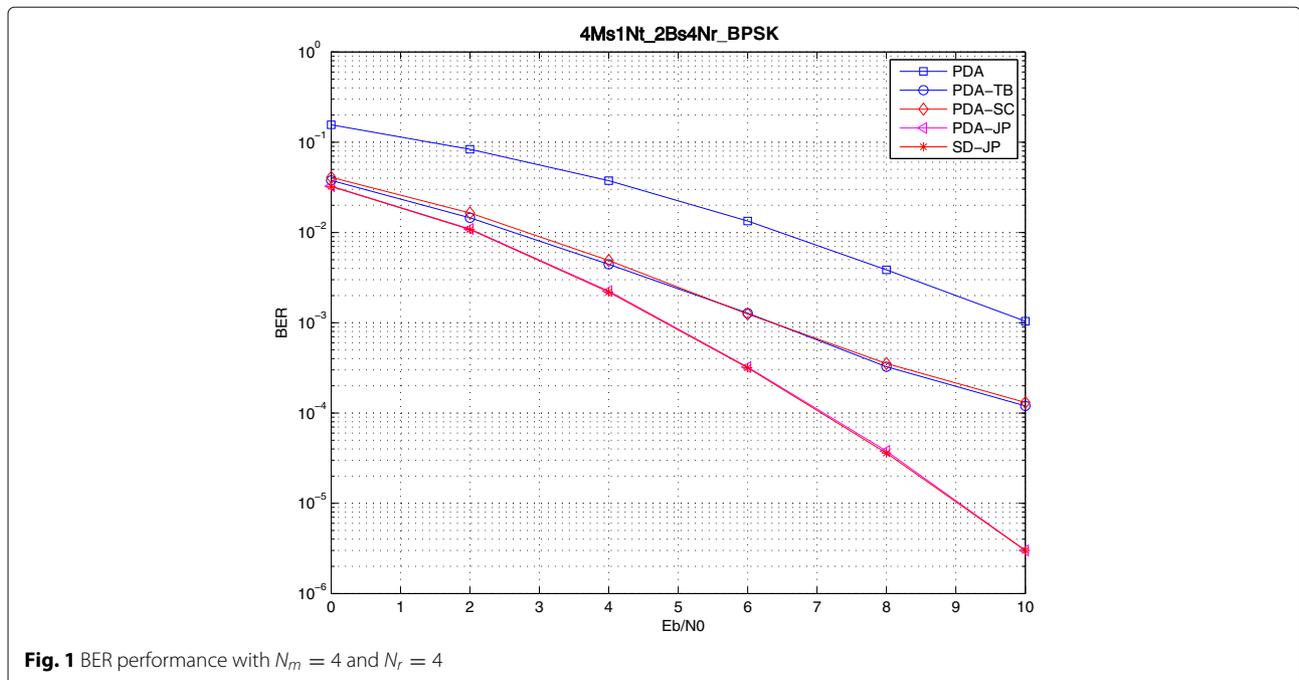


Fig. 1 BER performance with $N_m = 4$ and $N_r = 4$

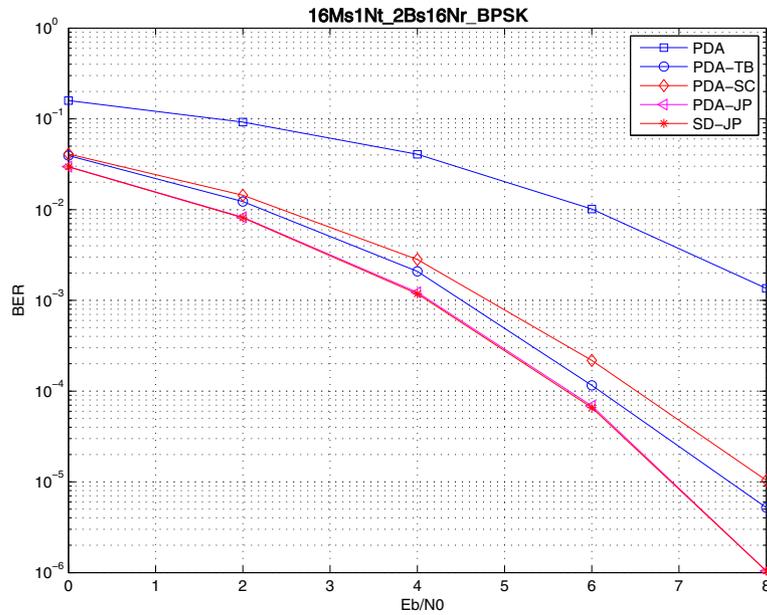


Fig. 2 BER performance with $N_m = 16$ and $N_r = 16$

conclude that the diversity gain of the base station dominates the total gain.

4.2 Complexity evaluation

The computational complexity of the proposed PDA-TB can be evaluated by simply comparing its complexity to PDA-SC and PDA-JP in a single (one inner and outer) iteration. The major computational cost of PDA-based

algorithms is the calculation of Σ_k^{-1} and the matrix multiplication of

$$\begin{pmatrix} R(\mathbf{w}) \\ I(\mathbf{w}) \end{pmatrix}^\top \Sigma_k^{-1} \begin{pmatrix} R(\mathbf{w}) \\ I(\mathbf{w}) \end{pmatrix}. \quad (32)$$

Using the Sherman-Morrison-Woodbury formulation-based “speed-up” techniques of [16], the computational cost of calculating Σ_k^{-1} can be reduced to $\mathcal{O}(4N_m N_t N_r^2)$

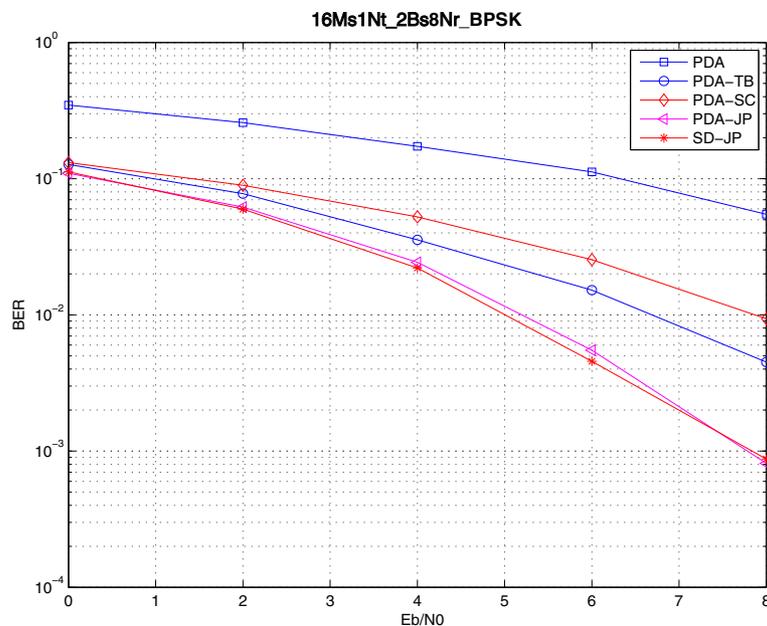


Fig. 3 BER performance with $N_m = 16$ and $N_r = 8$

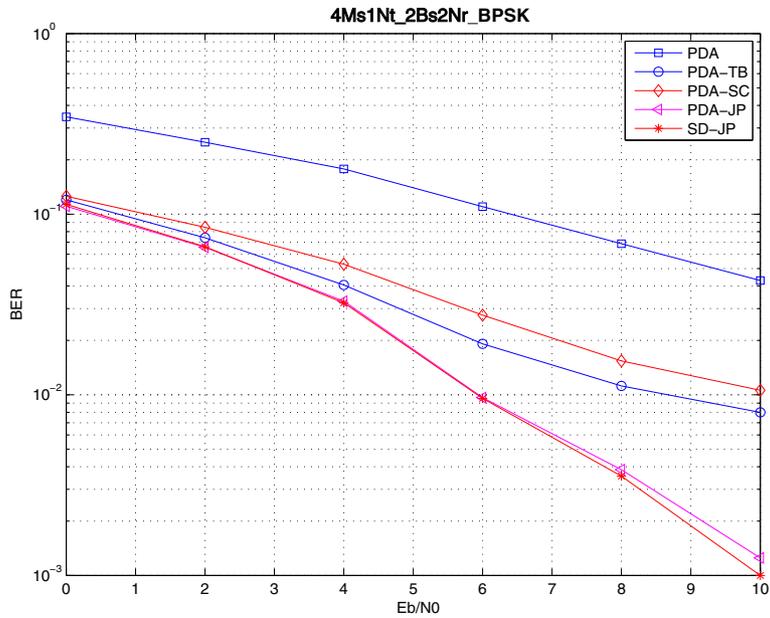


Fig. 4 BER performance with $N_m = 4$ and $N_r = 2$

real-valued operations (N_{RO}). Moreover, the calculation of (32) requires $\mathcal{O}(4MN_mN_tN_r^2 + 2MN_mN_tN_r) N_{RO}$. In summary, the computational cost of the proposed PDA-TB is $\mathcal{O}(4N_mN_tN_bN_r^2) + \mathcal{O}(4MN_mN_tN_bN_r^2 + 2MN_mN_tN_bN_r) N_{RO}$ per iteration.

The computational cost of PDA-SC is the same per iteration as PDA-TB, but PDA-JP has the complexity of

$\mathcal{O}(4N_mN_tN_b^2N_r^2) + \mathcal{O}(4MN_mN_tN_b^2N_r^2 + 2MN_mN_tN_bN_r) N_{RO}$ per iteration.

In addition, Fig. 8 shows that the average iteration number in turbo processing is rapidly reduced to 1 as E_b/N_0 increases and BER is below 10^{-4} . This implies that PDA-TB converges even at the first iteration $t = 0$ and then indicates that PDA-TB does not require more PDA

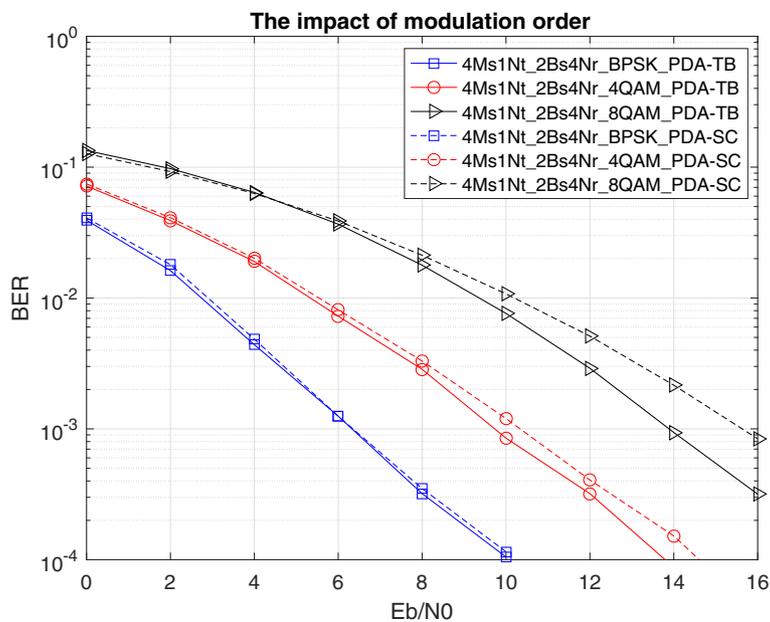


Fig. 5 The impact of modulation order

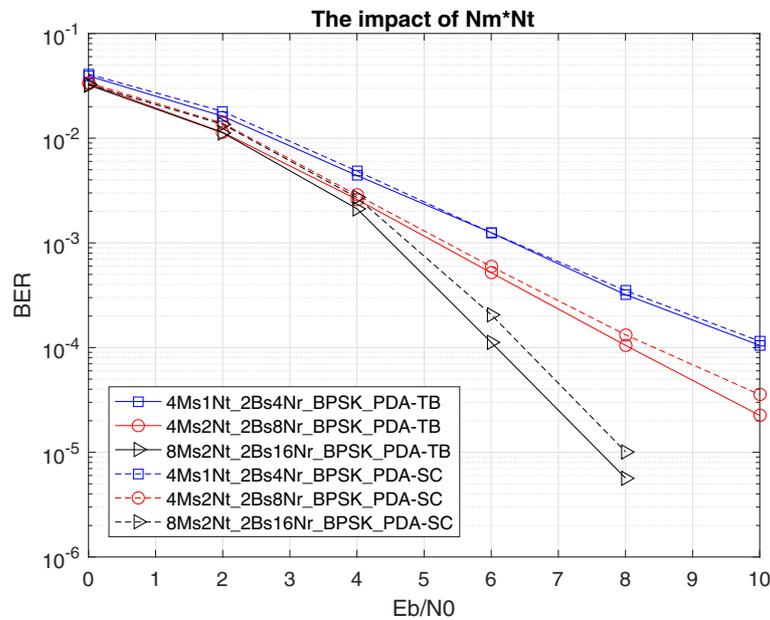


Fig. 6 The impact of total number of streams

computation than PDA-SC once BER reaches 10^{-4} or below. Meanwhile, the inner PDA iteration in PDA-TB is 0 while that in PDA-SC is set to be adaptive according to the convergence condition.

Moreover, PDA-TB does not have the step of soft combining employed by PDA-SC to make final decision. Instead, PDA-TB uses the output of PDA detector as the final decision once the algorithm converges. The possible

disadvantage in PDA-TB is that it might introduce the delay since it is sequential processing; however, PDA-SC is a parallel algorithm.

5 Conclusions

We propose a novel distributed PDA detector with turbo BS cooperations and show that PDA-TB outperforms existing PDA-SC in severe interference conditions. This

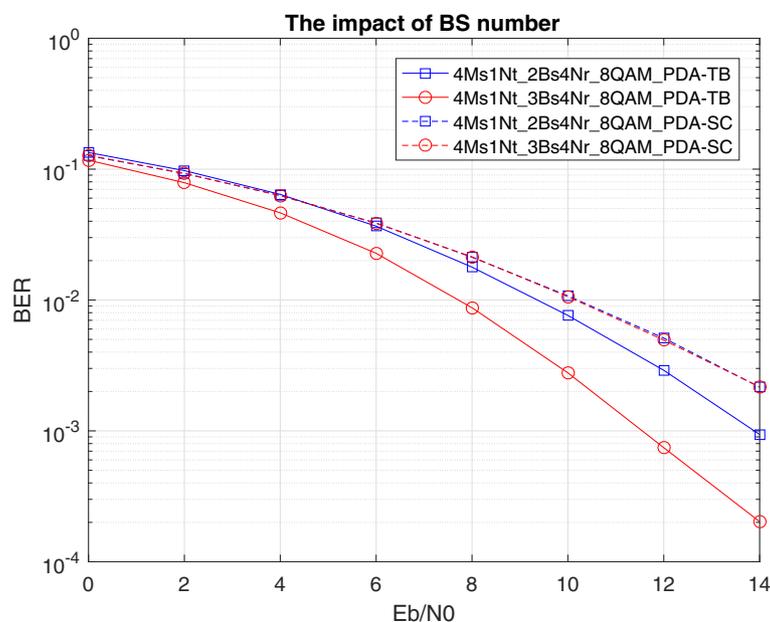


Fig. 7 The impact of BS number

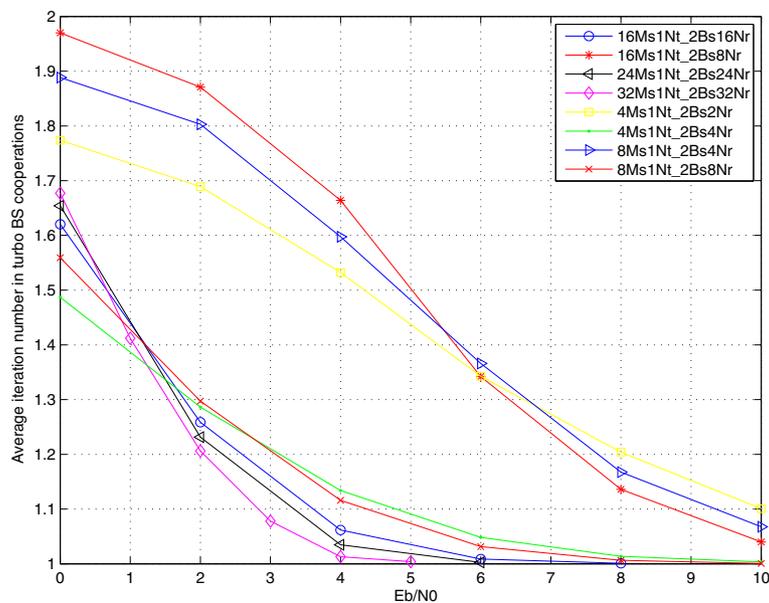


Fig. 8 Average turbo iteration number in PDA-TB

improvement is due to the appropriate manipulation of the a priori probability. The future direction will be complexity reduction for the distributed PDA detector.

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Authors' contributions

YY and HW contributed to the conception and design of the study. YY and GL contributed to the acquisition of data and simulation. YY, GL, and HW contributed to the analysis and interpretation of simulation data. All authors read and approved the final manuscript.

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Competing interests

The authors declare that they have no competing interests.

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